

A. Component-Based Semantics of Caml Light

A.1 Global names

$$id \llbracket GN \rrbracket = \mathbf{id}('GN')$$
 (1)

$$id \llbracket \text{prefix } ON \rrbracket = \mathbf{id}(' \text{prefix } ON')$$
 (2)

$$typeid \llbracket LI \rrbracket = \mathbf{typeid}('LI')$$
 (3)

A.2 Constants

$$value \llbracket Int \rrbracket = Int$$
 (4)

$$value \llbracket Float \rrbracket = Float$$
 (5)

$$value \llbracket Char \rrbracket = \mathbf{char}('CH')$$
 (6)

$$value \llbracket String \rrbracket = String$$
 (7)

$$value \llbracket K \rrbracket = \mathbf{fold-poly}(\mathbf{variant}('K', \mathbf{tuple-empty}))$$
 (8)

$$value \llbracket \text{false} \rrbracket = \mathbf{false}$$
 (9)

$$value \llbracket \text{true} \rrbracket = \mathbf{true}$$
 (10)

$$value \llbracket [] \rrbracket = \mathbf{fold-poly}(\mathbf{variant}('[]', \mathbf{tuple-empty}))$$
 (11)

$$value \llbracket () \rrbracket = \mathbf{tuple-empty}$$
 (12)

A.3 Patterns

$$patt \llbracket LI \rrbracket = \mathbf{bind}(id \llbracket LI \rrbracket)$$
 (13)

$$patt \llbracket - \rrbracket = \mathbf{any}$$
 (14)

$$patt \llbracket P \text{ as } LI \rrbracket = \mathbf{patt-union}(patt \llbracket P \rrbracket, \mathbf{bind}(id \llbracket LI \rrbracket))$$
 (15)

$$patt \llbracket \langle P \rangle \rrbracket = patt \llbracket P \rrbracket$$
 (16)

$$patt \llbracket \langle P : T \rangle \rrbracket = \mathbf{patt-at-type}(patt \llbracket P \rrbracket, type \llbracket T \rrbracket)$$
 (17)

$$patt \llbracket P1 \mid P2 \rrbracket = \mathbf{prefer-over}(patt \llbracket P1 \rrbracket, patt \llbracket P2 \rrbracket)$$
 (18)

$$patt \llbracket K \rrbracket = \mathbf{unfold-variant-select}('K', \mathbf{only}(\mathbf{tuple-empty}))$$
 (19)

$$patt \llbracket [] \rrbracket = \mathbf{unfold-variant-select}('[]', \mathbf{only}(\mathbf{tuple-empty}))$$
 (20)

$$patt \llbracket C \rrbracket = \mathbf{only}()$$
 (21)

$$patt \llbracket KP \rrbracket = \mathbf{unfold-variant-select}('K', patt \llbracket P \rrbracket)$$
 (22)

$$patt \llbracket P1, P2... \rrbracket = \mathbf{patt-tuple} \llbracket P1, P2... \rrbracket$$
 (23)

$$patt\text{-tuple} \llbracket P1 \rrbracket = \mathbf{invert tuple-prefix}(patt \llbracket P1 \rrbracket, \mathbf{only}(\mathbf{tuple-empty}))$$
 (24)

$$patt\text{-tuple} \llbracket P1, P2... \rrbracket = \mathbf{invert tuple-prefix}(patt \llbracket P1 \rrbracket, patt\text{-tuple} \llbracket P2... \rrbracket)$$
 (25)

$$patt \llbracket \{ L1 = P1... \} \rrbracket = \mathbf{loose record}(patt\text{-map} \llbracket L1 = P1... \rrbracket)$$
 (26)

$$patt \llbracket \{ L1 = P1... ; \} \rrbracket = \mathbf{patt} \llbracket \{ L1 = P1... \} \rrbracket$$
 (27)

$$patt\text{-map} \llbracket L1 = P1 \rrbracket = \mathbf{map1}('L1', \mathbf{compose}(patt \llbracket P1 \rrbracket, \mathbf{abs assigned-value}))$$
 (28)

$$patt\text{-map} \llbracket L1 = P1 ; L2 = P2... \rrbracket = \mathbf{map-union}(patt\text{-map} \llbracket L1 = P1 \rrbracket, patt\text{-map} \llbracket L2 = P2... \rrbracket)$$
 (29)

$$patt \llbracket [P1] \rrbracket = patt \llbracket P1 :: [] \rrbracket$$
 (30)

$$patt \llbracket [P1 ; P2...] \rrbracket = patt \llbracket P1 :: [P2...] \rrbracket$$
 (31)

$$patt \llbracket [P1... ;] \rrbracket = patt \llbracket [P1...] \rrbracket$$
 (32)

$$patt \llbracket P1 :: P2 \rrbracket = \mathbf{unfold-variant-select}('::', \mathbf{invert tuple2}(patt \llbracket P1 \rrbracket, patt \llbracket P2 \rrbracket))$$
 (33)

A.4 Expressions

$$expr \llbracket V \rrbracket = \mathbf{instantiate-if-poly}(\mathbf{bound-value}(id \llbracket V \rrbracket))$$
 (34)

$$expr \llbracket C \rrbracket = value \llbracket C \rrbracket$$
 (35)

$$expr \llbracket \langle E \rangle \rrbracket = expr \llbracket E \rrbracket$$
 (36)

$$expr \llbracket \text{begin } E \text{ end} \rrbracket = expr \llbracket E \rrbracket$$
 (37)

$$expr \llbracket \langle E : T \rangle \rrbracket = \mathbf{typed}(expr \llbracket E \rrbracket, type \llbracket T \rrbracket)$$
 (38)

$$expr \llbracket E1, E2... \rrbracket = \mathbf{expr-tuple} \llbracket E1, E2... \rrbracket$$
 (39)

$$\mathbf{expr-tuple} \llbracket E1 \rrbracket = \mathbf{tuple-prefix}(expr \llbracket E1 \rrbracket, \mathbf{tuple-empty})$$
 (40)

$$\mathbf{expr-tuple} \llbracket E1, E2... \rrbracket = \mathbf{tuple-prefix}(expr \llbracket E1 \rrbracket, \mathbf{expr-tuple} \llbracket E2... \rrbracket)$$
 (41)

$$expr \llbracket KE \rrbracket = \mathbf{fold-poly}(\mathbf{variant}('K', expr \llbracket E \rrbracket))$$
 (42)

$$expr \llbracket E1 :: E2 \rrbracket = \mathbf{fold-poly}(\mathbf{variant}('::', \mathbf{tuple2}(expr \llbracket E1 \rrbracket, expr \llbracket E2 \rrbracket)))$$
 (43)

$$expr \llbracket [E1] \rrbracket = expr \llbracket E1 :: [] \rrbracket$$
 (44)

$$expr \llbracket [E1 ; E2...] \rrbracket = expr \llbracket E1 :: [E2...] \rrbracket$$
 (45)

$$\text{expr}[[E1... ;]] = \text{expr}[[E1...]] \quad (46)$$

$$\text{expr}[[[]]] = \text{array-empty} \quad (47)$$

$$\text{expr}[[[] E1 []]] = \text{array1}(\text{alloc}(\text{expr}[[E1]])) \quad (48)$$

$$\text{expr}[[[] E1 ; E2... []]] = \text{array-append}(\text{expr}[[[] E1 []]], \text{expr}[[[] E2... []]]) \quad (49)$$

$$\text{expr}[[[] [E1 ; E2... ;]]] = \text{expr}[[[] E1 ; E2... []]] \quad (50)$$

$$\text{expr}[[{ L1 = E1 }]] = \text{record1}('L1', \text{alloc}(\text{expr}[[E1]])) \quad (51)$$

$$\text{expr}[[{ L1 = E1 ; L2 = E2... }]] = \text{record-union}(\text{expr}[[{ L1 = E1 }]], \text{expr}[[{ L2 = E2... }]]) \quad (52)$$

$$\text{expr}[[L1 = E1... ;]] = \text{expr}[[L1 = E1...]] \quad (53)$$

$$\text{expr}[[E1E2]] = \text{apply}(\text{expr}[[E1]], \text{expr}[[E2]]) \quad (54)$$

$$\text{expr}[[- E1]] = \text{expr}[[\text{minus } E1]] \quad (55)$$

$$\text{expr}[[- . E1]] = \text{expr}[[\text{minus-float } E1]] \quad (56)$$

$$\text{expr}[[! E1]] = \text{expr}[[\text{prefix } ! E1]] \quad (57)$$

$$\text{expr}[[E1IOE2]] = \text{expr}[[\text{prefix } IOE1E2]] \quad (58)$$

$$\text{expr}[[E1 . L]] = \text{assigned-value}(\text{record-select}(\text{expr}[[E1]], 'L')) \quad (59)$$

$$\text{expr}[[E1 . L <- E2]] = \text{assign}(\text{record-select}(\text{expr}[[E1]], 'L'), \text{expr}[[E2]]) \quad (60)$$

$$\text{expr}[[E1 . (E2)]] = \text{expr}[[\text{vect_item } E1E2]] \quad (61)$$

$$\text{expr}[[E1 . (E2) <- E3]] = \text{expr}[[\text{vect_assign } E1E2E3]] \quad (62)$$

$$\text{expr}[[\text{not } E1]] = \text{not}(\text{expr}[[E1]]) \quad (63)$$

$$\text{expr}[[E1 \& E2]] = \text{if-true}(\text{expr}[[E1]], \text{expr}[[E2]], \text{false}) \quad (64)$$

$$\text{expr}[[E1 \&\& E2]] = \text{expr}[[E1 \& E2]] \quad (65)$$

$$\text{expr}[[E1 \text{ or } E2]] = \text{if-true}(\text{expr}[[E1]], \text{true}, \text{expr}[[E2]]) \quad (66)$$

$$\text{expr}[[E1 || E2]] = \text{expr}[[E1 \text{ or } E2]] \quad (67)$$

$$\text{expr}[[\text{if } E1 \text{ then } E2]] = \text{expr}[[\text{if } E1 \text{ then } E2 \text{ else } ()]] \quad (68)$$

$$\text{expr}[[\text{if } E1 \text{ then } E2 \text{ else } E3]] = \text{if-true}(\text{expr}[[E1]], \text{expr}[[E2]], \text{expr}[[E3]]) \quad (69)$$

$$\text{expr}[[\text{while } E1 \text{ do } E2 \text{ done}]] = \text{seq}(\text{while-true}(\text{expr}[[E1]], \text{effect}(\text{expr}[[E2]])), \text{tuple-empty}) \quad (70)$$

$$\text{expr}[[\text{for } LI = E1 \text{ to } E2 \text{ do } E3 \text{ done}]] = \text{apply-to-each}(\text{abs}(\text{bind}(id[[LI]]), \text{effect}(\text{expr}[[E3]])), \text{int-closed-interval}(\text{expr}[[E1]], \text{expr}[[E2]])) \quad (71)$$

$$\text{expr}[[\text{for } LI = E1 \text{ downto } E2 \text{ do } E3 \text{ done}]] = \text{apply-to-each}(\text{abs}(\text{bind}(id[[LI]]), \text{effect}(\text{expr}[[E3]])), \text{list-reverse}(\text{int-closed-interval}(\text{expr}[[E2]], \text{expr}[[E1]]))) \quad (72)$$

$$\text{expr}[[E1 ; E2]] = \text{seq}(\text{effect}(\text{expr}[[E1]]), \text{expr}[[E2]]) \quad (73)$$

$$\text{expr}[[E1 ; E2 ;]] = \text{expr}[[E1 ; E2]] \quad (74)$$

$$\text{expr}[[\text{match } E \text{ with } SM]] = \text{apply}(\text{prefer-over}(\text{abs}[[SM]], \text{abs}(\text{throw}('Match_failure'))), \text{expr}[[E]]) \quad (75)$$

$$\text{expr}[[\text{function } SM]] = \text{close}(\text{prefer-over}(\text{abs}[[SM]], \text{abs}(\text{throw}('Match_failure')))) \quad (76)$$

$$\text{expr}[[\text{fun } Ps1 \rightarrow E \mid Ps2 \rightarrow E...]] = \text{prefer-over}(\text{expr}[[\text{fun } Ps1 \rightarrow E]], \text{expr}[[\text{fun } Ps2 \rightarrow E...]]) \quad (77)$$

$$\text{expr}[[\text{fun } P1 P2 P3... \rightarrow E]] = \text{curry}(\text{expr}[[\text{fun } (P1 , P2) \rightarrow \text{fun } P3... \rightarrow E]]) \quad (78)$$

$$\text{expr}[[\text{fun } P1 P2 \rightarrow E]] = \text{curry}(\text{expr}[[\text{fun } (P1 , P2) \rightarrow E]]) \quad (79)$$

$$\text{expr}[[\text{fun } P1 \rightarrow E]] = \text{expr}[[\text{function } P1 \rightarrow E]] \quad (80)$$

$$\begin{aligned} \text{expr}[\text{try } E \text{ with } SM] = & \quad (81) \\ & \text{catch-else-throw}(\text{expr}[E], \text{restrict-domain}(\text{abs}[SM], \\ & \quad \text{bound-type}(\text{typeid}(' \text{exn}')))) \end{aligned}$$

$$\begin{aligned} \text{expr}[VD \text{ in } E] = & \quad (82) \\ & \text{scope}(\text{decl}[VD], \text{expr}[E]) \end{aligned}$$

A.5 Pattern matching

$$\begin{aligned} \text{abs}[P1 \rightarrow E1] = & \quad (83) \\ & \text{abs}(\text{patt}[P1], \text{expr}[E1]) \end{aligned}$$

$$\begin{aligned} \text{abs}[P1 \rightarrow E1 \mid P2 \rightarrow E2\dots] = & \quad (84) \\ & \text{prefer-over}(\text{abs}[P1 \rightarrow E1], \text{abs}[P2 \rightarrow E2\dots]) \end{aligned}$$

$$\begin{aligned} \text{abs}[\mid P1 \rightarrow E1\dots] = & \quad (85) \\ & \text{abs}[P1 \rightarrow E1\dots] \end{aligned}$$

A.6 Value definitions

$$\begin{aligned} \text{decl}[\text{let rec } LB\dots] = & \quad (86) \\ & \text{generalise-all}(\text{recursive-typed}(\text{bound-ids}[LB\dots], \\ & \quad \text{decl-mono}[LB\dots])) \end{aligned}$$

$$\begin{aligned} \text{decl}[\text{let } LB\dots] = & \quad (87) \\ & \text{decl}[LB\dots] \end{aligned}$$

$$\begin{aligned} \text{decl}[LB1 \text{ and } LB2\dots] = & \quad (88) \\ & \text{map-union}(\text{decl}[LB1], \text{decl}[LB2\dots]) \end{aligned}$$

$$\begin{aligned} \text{decl}[VP\dots = E] = & \quad (89) \\ & \text{generalise-all}(\text{decl-mono}[VP\dots = E]) \end{aligned}$$

$$\begin{aligned} \text{decl}[P = V] = & \quad (90) \\ & \text{generalise-all}(\text{decl-mono}[P = V]) \end{aligned}$$

$$\begin{aligned} \text{decl}[P = C] = & \quad (91) \\ & \text{generalise-all}(\text{decl-mono}[P = C]) \end{aligned}$$

$$\begin{aligned} \text{decl}[P = \text{function } SM] = & \quad (92) \\ & \text{generalise-all}(\text{decl-mono}[P = \text{function } SM]) \end{aligned}$$

$$\begin{aligned} \text{decl}[P = \text{fun } MM] = & \quad (93) \\ & \text{generalise-all}(\text{decl-mono}[P = \text{fun } MM]) \end{aligned}$$

$$\begin{aligned} \text{decl}[P = E] = & \quad (94) \\ & \text{decl-mono}[P = E] // \text{default} \end{aligned}$$

$$\begin{aligned} \text{decl-mono}[LB1 \text{ and } LB2\dots] = & \quad (95) \\ & \text{map-union}(\text{decl-mono}[LB1], \text{decl-mono}[LB2\dots]) \end{aligned}$$

$$\begin{aligned} \text{decl-mono}[P = E] = & \quad (96) \\ & \text{match}(\text{expr}[E], \text{prefer-over}(\text{patt}[P], \\ & \quad \text{abs}(\text{throw}(' \text{Match_failure}')))) \end{aligned}$$

$$\begin{aligned} \text{decl-mono}[VP\dots = E] = & \quad (97) \\ & \text{bind-value}(\text{id}[V], \text{expr}[\text{fun } P\dots \rightarrow E]) \end{aligned}$$

$$\begin{aligned} \text{bound-ids}[LB1 \text{ and } LB2\dots] = & \quad (98) \\ & \text{map-union}(\text{bound-ids}[LB1], \text{bound-ids}[LB2\dots]) \end{aligned}$$

$$\begin{aligned} \text{bound-ids}[LI = E] = & \quad (99) \\ & \text{map1}(\text{id}[LI], \text{unknown-type}) \end{aligned}$$

$$\begin{aligned} \text{bound-ids}[(LI : TE) = E] = & \quad (100) \\ & \text{map1}(\text{id}[LI], \text{type}[TE]) \end{aligned}$$

$$\begin{aligned} (\text{bound-ids}[\mid P = E] \text{ otherwise unspecified}) & \quad (101) \\ & \text{bound-ids}[VP\dots = E] = \\ & \quad \text{map1}(\text{id}[V], \text{unknown-type}) \end{aligned}$$

A.7 Types

$$\begin{aligned} \text{type}[LI] = & \quad (102) \\ & \text{bound-type}(\text{typeid}[LI]) \end{aligned}$$

$$\begin{aligned} \text{type}[TE1 \rightarrow TE2] = & \quad (103) \\ & \text{depends}(\text{type}[TE1], \text{type}[TE2]) \end{aligned}$$

$$\begin{aligned} \text{type}[(TE)] = & \quad (104) \\ & \text{type}[TE] \end{aligned}$$

$$\begin{aligned} \text{type}[TELI] = & \quad (105) \\ & \text{instantiate-type}(\text{type}[LI], \text{list1}(\text{type}[TE])) \end{aligned}$$

$$\begin{aligned} \text{type}[(TE1, TE2\dots) LI] = & \quad (106) \\ & \text{instantiate-type}(\text{type}[LI], \text{list}[TE1, TE2\dots]) \end{aligned}$$

$$\begin{aligned} \text{type}[? LI] = & \quad (107) \\ & \text{typevar}(' LI') \end{aligned}$$

$$\begin{aligned} \text{type}[TE1 * TE2] = & \quad (108) \\ & \text{tuple2}(\text{type}[TE1], \text{type}[TE2]) \end{aligned}$$

$$\begin{aligned} \text{type}[TE1 * TE2 * TE3\dots] = & \quad (109) \\ & \text{tuple-prefix}(\text{type}[TE1], \text{type}[TE2 * TE3\dots]) \end{aligned}$$

$$\begin{aligned} \text{list}[TE1, TE2] = & \quad (110) \\ & \text{list2}(\text{type}[TE1], \text{type}[TE2]) \end{aligned}$$

$$\begin{aligned} \text{list}[TE1, TE2, TE3\dots] = & \quad (111) \\ & \text{list-prefix}(\text{type}[TE1], \text{list}[TE2, TE3\dots]) \end{aligned}$$

A.8 Type definitions

$$\begin{aligned} \text{decl}[LI == TE] = & \quad (112) \\ & \text{typedef}(\text{typeid}[LI], \text{type}[TE]) \end{aligned}$$

$$\begin{aligned} \text{decl}[TPS LI == TE] = & \quad (113) \\ & \text{typedef}(\text{typeid}[LI], \\ & \quad \text{type-abs}(\text{typevar-list}[TPS], \text{type}[TE])) \end{aligned}$$

$$\begin{aligned} \text{decl}[TPS LI = \{ LD\dots \}] = & \quad (114) \\ & \text{typedef}(\text{typeid}[LI], \\ & \quad \text{type-abs}(\text{typevar-list}[TPS], \text{record}(\text{map}[LD\dots]))) \end{aligned}$$

$decl\llbracket LI = LD\dots \rrbracket =$ (115)
typedef(*typeid* $\llbracket LI \rrbracket$,
record(*map* $\llbracket LD\dots \rrbracket$))

$decl\llbracket TPS\ LI = CD\dots \rrbracket =$ (116)
typedef(*typeid* $\llbracket LI \rrbracket$, **rectype**(*typeid* $\llbracket LI \rrbracket$,
type-abs(*typevar-list* $\llbracket TPS \rrbracket$, **variant**(*map* $\llbracket CD\dots \rrbracket$))))

$decl\llbracket LI = CD\dots \rrbracket =$ (117)
typedef(*typeid* $\llbracket LI \rrbracket$, **rectype**(*typeid* $\llbracket LI \rrbracket$,
variant(*map* $\llbracket CD\dots \rrbracket$)))

typevar-list $\llbracket ' LI \rrbracket =$ (118)
list1(*typevar* (' *LI*'))

typevar-list $\llbracket (' LI) \rrbracket =$ (119)
typevar-list $\llbracket ' LI \rrbracket$

typevar-list $\llbracket (' LI1 , ' LI2\dots) \rrbracket =$ (120)
list-prefix(*typevar* (' *LI1*'), *typevar-list* $\llbracket (' LI2\dots) \rrbracket$)

map $\llbracket LI : TE \rrbracket =$ (121)
map1(' *LI*', **variable**(*type* $\llbracket TE \rrbracket$))

map $\llbracket mutable\ LI : TE \rrbracket =$ (122)
map1(' *LI*', **variable**(*type* $\llbracket TE \rrbracket$))

map $\llbracket LD1 ; LD2\dots \rrbracket =$ (123)
map-union(*map* $\llbracket LD1 \rrbracket$, *map* $\llbracket LD2\dots \rrbracket$)

map $\llbracket K \rrbracket =$ (124)
map1(' *K*', **tuple-empty**)

map $\llbracket K\ of\ TE \rrbracket =$ (125)
map1(' *K*', *type* $\llbracket TE \rrbracket$)

map $\llbracket CD1 \mid CD2\dots \rrbracket =$ (126)
map-union(*map* $\llbracket CD1 \rrbracket$, *map* $\llbracket CD2\dots \rrbracket$)

A.9 Module implementations

decl-impl $\llbracket IP ; ; \dots \rrbracket =$ (127)
accum(*decl* $\llbracket IP \rrbracket$, *decl-impl* $\llbracket \dots \rrbracket$)

decl-impl $\llbracket \rrbracket =$ (128)
map-empty

decl $\llbracket E \rrbracket =$ (129)
seq(**print**(*expr* $\llbracket E \rrbracket$), **map-empty**)

decl $\llbracket type\ TD \rrbracket =$ (130)
decl $\llbracket TD \rrbracket$

decl $\llbracket type\ TD1\ and\ TD2\dots \rrbracket =$ (131)
map-union(*decl* $\llbracket TD1 \rrbracket$, *decl* $\llbracket type\ TD2\dots \rrbracket$)

decl $\llbracket exception\ CD \rrbracket =$ (132)
typedef(*typeid* (' *exn*'), **variant-type-extend**
(**bound-type**(*typeid* (' *exn*')), *map* $\llbracket CD \rrbracket$))

decl $\llbracket exception\ CD1\ and\ CD2\dots \rrbracket =$ (133)
accum(*decl* $\llbracket exception\ CD1 \rrbracket$, *decl* $\llbracket exception\ CD2\dots \rrbracket$)

decl $\llbracket D \rrbracket =$ (134)
map-empty

prog $\llbracket IMPL \rrbracket =$ (135)
scope(**caml-light-library**, *decl-impl* $\llbracket IMPL \rrbracket$)